Short note

Quadrupole moment measurement of the highly deformed $\pi g_{9/2} \otimes u h_{11/2}$ band in ${}^{130}{ m Pr}$

F.G. Kondev¹, M.A. Riley¹, T.B. Brown¹, R.M. Clark², M. Devlin³, P. Fallon², D.J. Hartley¹, I.M. Hibbert^{4,a}, D.T. Joss⁵, D.R. LaFosse^{3,b}, R.W. Laird¹, F. Lerma³, M. Lively¹, P.J. Nolan⁵, N.J. O'Brien⁴, E.S. Paul⁵, J. Pfohl¹, D.G. Sarantites³, R.K. Sheline¹, S.L. Shepherd⁵, J. Simpson⁶, R. Wadsworth⁴

¹ Department of Physics, Florida State University, Tallahassee, FL 32306, USA

² Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA

³ Department of Chemistry, Washington University, St. Louis, MO 63130, USA

⁴ Department of Physics, University of York, Heslington, York Y01 5DD, UK

⁵ Oliver Lodge Laboratory, University of Liverpool, Liverpool L69 7ZE, UK

 $^{6}\,$ CCLRC, Daresbury Laboratory, Daresbury, Warrington WA4 4AD, UK

Received: 23 April 1998 Communicated by B. Herskind

Abstract. The quadrupole moment for the $\pi g_{9/2} \otimes \nu h_{11/2}$ band in the ¹³⁰Pr nucleus has been measured using the Doppler-shift attenuation method. A centroid shift analysis was carried out and a value of $Q_0=6.1\pm0.4~eb$, corresponding to an axial prolate deformation of $\beta_2=0.35(3)$, has been determined. This is the first direct experimental confirmation of the deformation-driving character of the $\pi g_{9/2}$ orbital in an odd-odd nucleus in the A~135 superdeformed region.

PACS. 21.10.Tg Lifetimes – 21.10.Re Collective levels – 23.20.Lv Gamma transitions and level energies – 27.60.+j $90 \le A \le 149$

The stabilization of nuclear shapes in the so-called "superdeformed" second minimum of the potential energy is generally associated with a delicate interplay between the large shell gaps in the nucleon single-particle spectrum of states for high quadrupole deformation values and the occupation of high-j, low- Ω intruder orbitals. For nuclei around A~135, the occupation of one or more $i_{13/2}$ neutrons is thought to have a strong polarization effect on the nuclear shape [1,2]. However, it has been recently shown that certain strongly coupled bands, built upon the $9/2^{+}[404] (g_{9/2})$ proton orbital, in the odd-Z ¹³¹Pr [3] and ¹³³Pm [4] isotopes, exhibit high dynamical moment-ofinertia values, as well as quadrupole deformations, comparable to the values found for highly deformed structures in the A~135 region which involve $i_{13/2}$ neutrons. Bands involving the same $\pi g_{9/2}$ orbital have also been recently reported in the odd-odd 130 Pr [5] and 132 Pr [6] isotopes,

however, direct confirmation of their high deformation values from lifetime measurements have not previously been presented.

The current work reports on lifetime measurements for the $\pi g_{9/2} \otimes \nu h_{11/2}$ band in the ¹³⁰Pr nucleus [5], together with complementary results for the previously studied $\pi g_{9/2}$ band in ¹³¹Pr [3]. The aim was to establish the relative quadrupole deformations associated with these structures and hence clarify the polarization effect towards higher deformation for bands involving the $\pi g_{9/2}$ orbital. Analysis of data for normally deformed yrast structures in these nuclei [3,7,8] is also included for comparison.

The experiment was performed at the 88-Inch Cyclotron at the Lawrence Berkeley National Laboratory, where the high efficiency and resolving power of the GAM-MASPHERE γ -ray spectrometer array [9] were combined with the selectivity of the MICROBALL charged-particle detector system [10]. The ³⁵Cl+¹⁰⁵Pd fusion-evaporation reaction at a beam energy of 173 MeV was used. The target consisted of an enriched (up to 95%) ¹⁰⁵Pd foil of thickness 1 mg/cm² mounted on a 17 mg/cm² Au backing. The 2α particle channel (1.6% of the total data) contained 21×10^6 threefold or higher Compton-suppressed coinci-

Correspondence to: kondev@nucott.physics.fsu.edu

^a *Present address:* Oliver Lodge Laboratory, University of Liverpool, Liverpool L69 7ZE, UK

^b Present address: State University of New York at Stony Brook, NY 11794, USA



Fig. 1. The experimental and calculated $F(\tau)$ values as a function of γ -ray energy for selected bands in ¹³⁰Pr and ¹³¹Pr. Calculated curves are shown as solid lines and correspond to the best fit to the data

dence events. The ¹³⁰Pr nucleus (2 α 2n channel) accounted for about 36% of the 2 α data set and the $\pi g_{9/2} \otimes \nu h_{11/2}$ band was populated at a level of ~4% of the total 2 α 2n cross section. The $\pi g_{9/2}$ band in ¹³¹Pr received a substantial population (~15%) in the 2 α 1n channel, which accounted for ~37% of the 2 α events.

The data were sorted off-line into a number of twodimensional matrices in which one axis consisted of a group of detectors either at "forward" $(31.7^{\circ} \text{ and } 37.4^{\circ})$ or "backward" $(142.6^{\circ} \text{ and } 148.3^{\circ})$ angles, while the other axis contained coincident detectors at any angle. Onedimensional spectra were constructed by summing gates on the cleanest, fully stopped transitions at the bottom of the band of interest and projecting the events onto the "forward" and "backward" axes, respectively. The fractional Doppler shift, $F(\tau)$, was extracted for each γ -ray transition from these spectra using the centroid-shift technique [11]. Gating on transitions above the level of interest was also tried in order to eliminate the effect of side feeding, but the limited statistics of the resultant spectra were not sufficient to make this approach meaningful. The experimental $F(\tau)$ values for the highly deformed bands in 130 Pr and 131 Pr are shown in Fig. 1 (circles), as a function of γ -ray energy. In order to illustrate the deformation differences between the highly deformed and normally deformed structures, the $F(\tau)$ values for the $\pi h_{11/2} \otimes \nu d_{5/2}$ (¹³⁰Pr [7,8]) and $\pi h_{11/2}$ (¹³¹Pr [3]) bands are also plotted (triangles) in Fig. 1.

The average quadrupole moments, Q_0 , were extracted through a χ^2 -minimization fit of the experimental $F(\tau)$ data points to the values computed using the code FITF-TAU [12]. The lifetime of the in-band levels was related to Q_0 (assumed to be constant within the whole band) using rotational model formulae [13]. The stopping powers were calculated using the 1995 version of the code TRIM [14] and multiple scattering corrections were introduced using the prescription given by Blaugrund [15]. The side feeding into each state was modeled according to the experimental in-band intensity profile by assuming a rotational cascade of three transitions with the same Q_0 as the in-band states. For the strongly coupled bands, the effect of additional $I \rightarrow I-1$ branches on the partial level lifetime has been taken into account using the experimen-

Table 1. Quadrupole moments and deformations extracted for selected bands in $^{130}\mathrm{Pr}$ and $^{131}\mathrm{Pr}$

Nucleus	$Configuration^{(1)}$	$Q_0, eb [\beta_2]$		
		$\operatorname{present}^{(2)}$	previous	ref.
$^{130}\mathrm{Pr}$	$\pi g_{9/2} \otimes u h_{11/2}$	6.1(5)[0.35(3)]		
	$\pi h_{11/2} \otimes u d_{5/2}$	3.4(2)[0.20(1)]		
$^{131}\mathrm{Pr}$	$\pi g_{9/2}$	5.3(4)[0.31(2)]	5.5(8)[0.32(5)]	[3]
	$\pi h_{11/2}$	3.3(2)[0.19(1)]	3.9(3)[0.23(2)]	[3]

⁽¹⁾ Configurations are taken from refs. [3,5,7,8]; $\pi g_{9/2}$: 9/2⁺[404], $\pi h_{11/2}$: 3/2⁻[541], $\nu h_{11/2}$: 7/2⁻[523], $\nu d_{5/2}$: 5/2⁺[402]

(2) The quoted absolute errors are subject to a 15-25% systematic error, as explained in the text.

tally determined branching ratios. Table 1 summarizes the extracted Q_0 values, as well as the quadrupole deformations, β_2 , deduced by assuming an axially symmetric prolate shape with no hexadecapole deformation [16]. A value of $\beta_2=0.35(3)$, deduced for the highly deformed $\pi g_{9/2} \otimes \nu h_{11/2}$ configuration in ¹³⁰Pr, is consistent with the prediction made using total Routhian surface (TRS) calculations [5]. The results obtained for the bands in ¹³¹Pr are in agreement with those reported previously [3] (see Table 1). It should be emphasized, that although the uncertainties in the stopping powers and the modeling of the side feeding may contribute an additional systematic error of 15–25% in the absolute Q_0 values, the relative deformations can be considered to be accurate to 5–10%, since the bands were studied under the same conditions.

The present results show that the quadrupole deformation of the $\pi g_{9/2} \otimes \nu h_{11/2}$ band in ¹³⁰Pr is similar or perhaps slightly larger to that found for the highly deformed $\pi g_{9/2}$ band in ¹³¹Pr, and that it is much greater than the value deduced for structures where the $\pi g_{9/2}$ orbital is not involved. Many more highly deformed bands, formed by the coupling of different neutron orbitals to the $\pi g_{9/2}$ proton, are expected in odd-odd nuclei in this mass region. The observation of these structures and the measurement of their detailed properties remain a challenge for further studies.

The authors wish to extend their thanks to the staff of the LBNL GAMMASPHERE facility for their assistance during the experiment. The software support of D.C. Radford and H.Q. Jin is also greatly appreciated. Support for this work was provided by the U.S. Department of Energy under Contract No. DE-AC03-765F00098 and Grant No. DE-FG02-88ER-40406, the National Science Foundation, the State of Florida and the U.K. Engineering and Physical Sciences Research Council. MAR and JS acknowledge the receipt of a NATO Collaborative Research Grant.

References

- 1. R. Wyss et al., Phys. Lett. B215, 211 (1988)
- A.V. Afanasjev and I. Ragnarsson, Nucl. Phys. A608, 176 (1996)

F.G. Kondev et al.: Quadrupole moment measurement of the highly deformed $\pi g_{9/2} \otimes \nu h_{11/2}$ band in ¹³⁰Pr 251

- 3. A. Galindo-Uribarri *et al.*, Phys. Rev. **C50**, R2655 (1994)
- 4. A. Galindo-Uribarri et~al., Phys. Rev. ${\bf C54},\,1057$ (1996)
- 5. T.B. Brown *et al.*, Phys. Rev. **C56**, R1210 (1997)
- 6. D.J. Hartley *et al.*, Phys. Rev. **C55**, R985 (1997)
- 7. R. Ma et al., Phys. Rev. C37, 1926 (1988)
- C.M. Petrache et al., DFPD/NP/47, 1997 (unpublished)
 I.Y. Lee, in Proceedings of the Workshop on Gammasphere
- Physics, Berkeley, 1995, edited by M.A. Deleplanque, I.Y.
 Lee and A.O. Macchiavelli, (World Scientific Publishing
 Co. Pte. Ltd, 1996), p. 50.; I.Y. Lee, Nucl. Phys. A520, 614c (1990)
- D.G. Sarantites *et al.*, Nucl. Instrum. and Meth. in Phys. Res. A381, 418 (1996)

- T.K. Alexander and J.S. Forster, *Advances in Nuclear Physics*, edited by M. Baranger and E. Vogt (Plenum, New York 1978), Vol.10, p.197
- E.F. Moore et al., in Proceedings of the Conference on Nuclear Structure at the Limits, Argonne, Illinois, 1996, (ANL/PHY-97/1) p.72
- A. Bohr and B.R. Mottelson, Nuclear Structure (W.A. Benjamin, 1975), Vol. II, p.45
- J.F. Ziegler, J.P. Biersack and U. Littmark, *The Stopping* and Range of Ions in Solids (Pergamon, New York, 1985);
 J.F. Ziegler (private communication)
- 15. A.E. Blaugrund, Nucl. Phys. 88, 501 (1966)
- 16. K.E.G. Löbner et al., Nucl. Data Tables A7, 495 (1970)